

*The 5<sup>th</sup> International Symposium on Negative Ions, Beams and Sources  
12-16, September 2016, St. Anne's College, Oxford, UK*

# **Study of energy relaxation processes of the surface produced negative ions by using the 3D3V PIC simulation**

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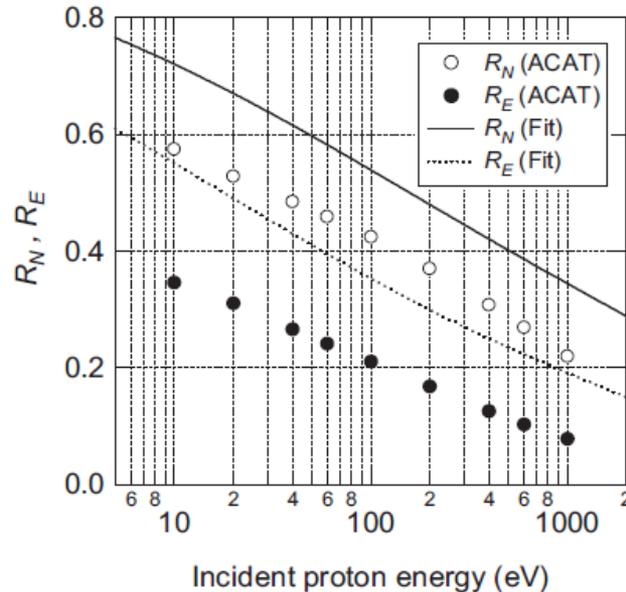
## **4. Summary and future plan**

# Introduction (I)

- A negative ion source which can produce negative ion beams with **high power** and **long pulse** is the key component for the negative ion based NBI system for plasma heating and current drive of magnetic fusion reactors.
- For the design and development of such a negative ion source, the study of the **H<sup>-</sup> ion beam optics** is one of the crucial issues since the H<sup>-</sup> ion beams with **poor beam optics** will cause the **excessive heat loads** and **the breakdown** in the accelerator.
- In the present tandem-type negative ion sources, **surface production** is dominant for the H<sup>-</sup> ion production process. In surface production, the **H<sup>+</sup> ions and/or H atoms impinge on the PG surface** with the low work function, and are converted to H<sup>-</sup> ions. Since the H atoms are generated mainly by **dissociation of the H<sub>2</sub> molecules of the Frank-Condon process**, or the H<sup>+</sup> ions are **accelerated through the sheath**, these incident H atoms and/or H<sup>+</sup> ions are considered to have the **energy of a few eV**.

# Introduction (II)

- From particle simulations and semi-empirical formulas, the **energy reflection coefficient** for the low energy of a few eV is estimated to be around **0.5**. Therefore, the **surface produced H<sup>-</sup> ions** are considered to be launched with the **initial energy of 1 ~ 2 eV**.
- However, it is well-known that **negative ion beams** in the tandem-type negative ion source have **good beam optics**. From the measured emittance of the H<sup>-</sup> ion beam, one can estimate the **H<sup>-</sup> ion temperature** to be **0.1 eV** of the order of the **magnitude**, and it is reported that the **measured H<sup>-</sup> ion temperature** is **0.1 eV**.



M. Wada, M. Bacal, T. Kasuya, S. Kato, T. Kenmotsu and M. Sasao, *AIP conference proceedings*, **1515**, 59-65 (2013).

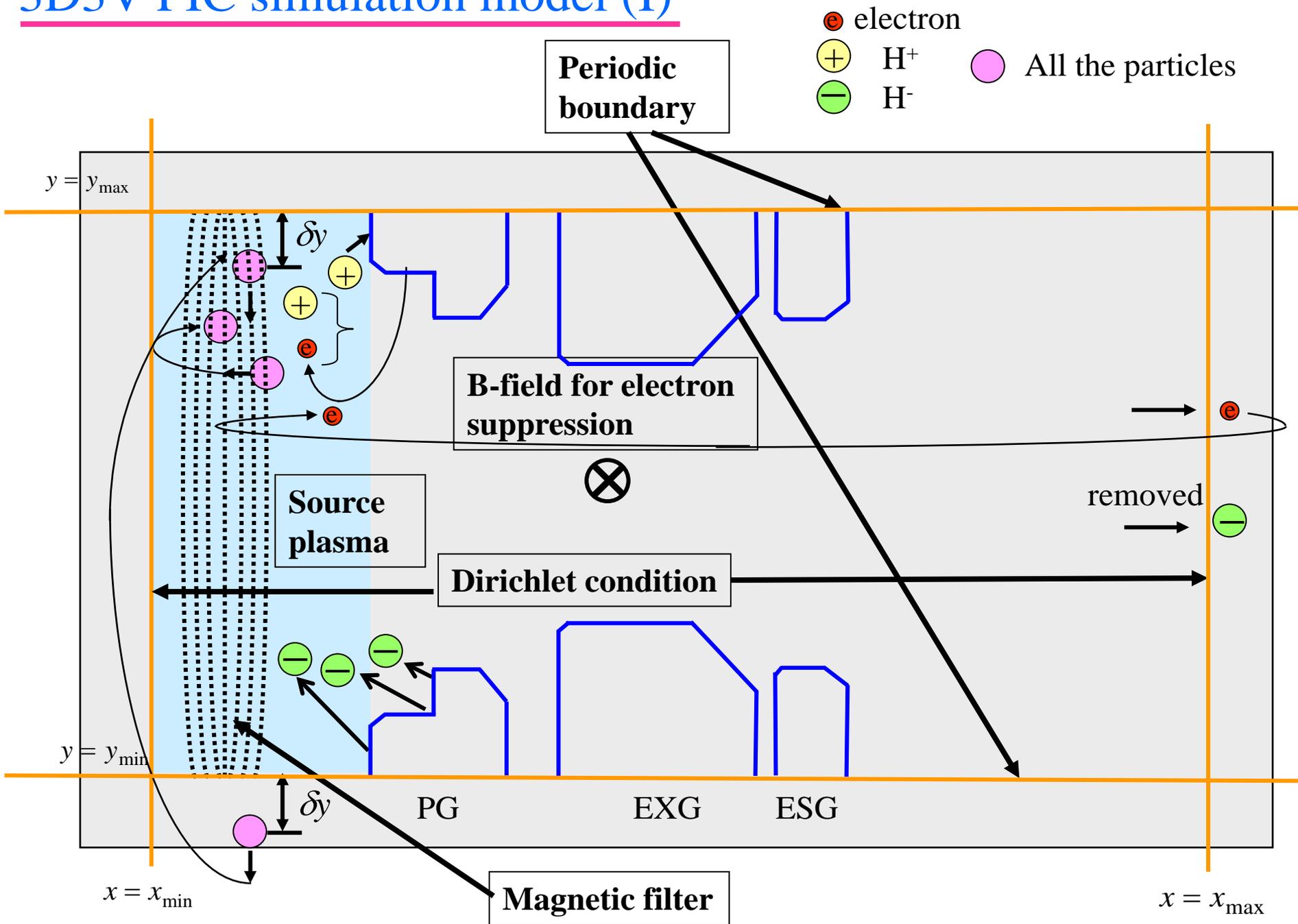
FIGURE 6. Comparison of  $R_N$  and  $R_E$  calculated by ACAT code to those obtained from empirical formulas introduced in reference [14].

# Introduction (III)

- The **energy relaxation** of  $H^-$  ions is possible reason for the **good beam optics** of the **surface produced  $H^-$  ions**.
- The previous studies by using a three-dimensional Monte Carlo simulation show that the **Coulomb collision** with the  $H^+$  ions and the **charge exchange collision** with the H atoms ( $H^- + H \rightarrow H + H^-$ ) contribute to the energy relaxation of  $H^-$  ions. However, the background plasma is not solved self-consistently. Moreover, the electric field for the  $H^-$  extraction has not been taken into account.
- Recently, the study of the  $H^-$  energy relaxation due to the Coulomb collision has been carried out by using the 2D3V PIC simulation<sup>1</sup>. Since the **PIC simulation** can **solve** the **plasma** and the **electric field self-consistently**, it is useful to clarify the physical mechanism of  $H^-$  ion extraction and beam optics.
- In this study, we extend to the **3D3V PIC simulation** model, and **verify** the **energy relaxation processes** in detail. Moreover, the **effect of the energy relaxation processes** on the  **$H^-$  ion beam optics** is investigated.

1. I. Goto, K. Miyamoto, S. Nishioka, S. Mattei, J. Lettry, S. Abe, and A. Hatayama, *Rev. Sci. Instrum.*, **87** 02B918/1-3 (2016).

# 3D3V PIC simulation model (I)



# 3D3V PIC simulation model (II)

## Main physical parameters in the source region

Physical parameters	Symbol	Value
Electron temperature	$T_e$	1 eV
Hydrogen ion temperature	$T_{H^+}$ $T_{H^-}$	0.25 eV 0.25 eV (volume production) 1.50 eV (surface production)
Electron density	$n_e$	$10^{18}\text{m}^{-3}$
Electron Debye length	$\lambda_{De}$	$7.4 \times 10^{-6}$ m
Electron plasma frequency	$\omega_{pe}$	$5.6 \times 10^{10}$ rad/s

- Initial number of super-particles :  $10^7$  of the order of the magnitude
- The number of numerical grid is  $433 \times 153 \times 153$  in the  $x$ ,  $y$  and  $z$  directions respectively, which corresponds to  $54 \text{ mm} \times 19 \text{ mm} \times 19 \text{ mm}$  in real size.
- Electrons,  $H^+$  ions, and volume produced  $H^-$  ions are assumed to be launched with Maxwellian distributions. The surface produced  $H^-$  ions are assumed to be launched with half-Maxwellian distribution.

## 3D3V PIC simulation model (III)

• The following collision processes are taken into account as the energy relaxation processes of  $H^-$  ions.

### 1) Coulomb collision

A binary collision model by the Monte Carlo method is used.

### 2) Charge exchange collision ( $H^-$ (fast) + H (slow) $\rightarrow$ $H^-$ (slow) + H (fast))

The null collision model is used.

$$n_{H_2} = 1.88 \times 10^{19} \text{ m}^{-3} \quad (p_{H_2} = n_{H_2} k T_{H_2}, p_{H_2} = 0.3 \text{ Pa}, T_{H_2} = 0.1 \text{ eV})$$

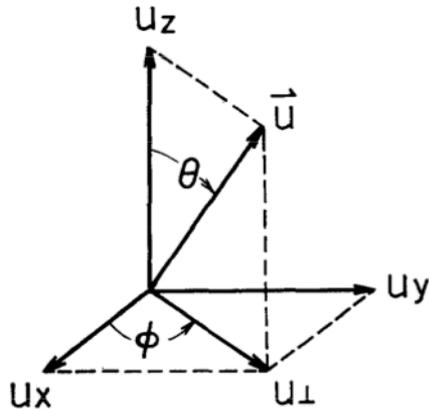
$$n_H/n_{H_2} = 0.5 \quad (\text{U. Fantz, et al., } Rev. Sci. Instrum., \mathbf{77}, 03A516 (2006).)$$

$$n_H = 9.38 \times 10^{19} \text{ m}^{-3}$$

• In the present model, the mutual neutralization ( $H^- + H^+ \rightarrow H + H$ ) is taken into account as  $H^-$  ion destruction process.

# Binary collision model by the Monte Carlo method

A binary collision model (BCM)<sup>2</sup> by the Monte Carlo method is applied to the Coulomb collision with the H<sup>+</sup> ions.



$$\Phi = 2\pi\delta_1$$

$$\theta = 2 \arctan \delta_2$$

$$\langle \delta_2 \rangle = 0$$

$$\langle \delta_2^2 \rangle = \frac{n_L (e_1 e_2)^2 \ln \Lambda}{8\pi \epsilon_0^2 m_{\alpha\beta} u^3} \Delta t$$

$\delta_1, \delta_2$  : uniform random number

$n_L$  : particle density

$m_{\alpha\beta}$  : reduced mass

$\ln \Lambda$  : Coulomb logarithm

$\Delta t$  : time step

$$\Delta u_x = \frac{u_x}{u_{\perp}} u_z \sin \theta \cos \Phi - \frac{u_y}{u_{\perp}} u \sin \theta \sin \Phi - u_x (1 - \cos \theta)$$

$$\Delta u_y = \frac{u_y}{u_{\perp}} u_z \sin \theta \cos \Phi - \frac{u_x}{u_{\perp}} u \sin \theta \sin \Phi - u_y (1 - \cos \theta)$$

$$\Delta u_z = -u_{\perp} \sin \theta \cos \Phi - u_z (1 - \cos \theta)$$

$$u_{\perp} = \sqrt{u_x^2 + u_y^2}$$

# Model of the charge exchange collision

- As for the charge exchange collision, an electron moves from the surface produced  $H^-$  ion (fast ions) to a slow H atom, which then leaves behind a slow scattered  $H^-$  ion.
- This slow  $H^-$  ion is scattered isotropically: the scattering angles are randomly chosen as

$$\theta = \pi U_1, \Phi = 2\pi U_2 \quad (U_2, U_3: \text{a uniform random number})$$

- The speed of the scattered  $H^-$  ion is chosen to match the H atom velocity distribution ( $T_H = 0.1$  eV).
- Whether the charge exchange collision occurs or not is determined by using the null collision model<sup>3</sup>. In the present model, the mutual neutralization ( $H^- + H^+ \rightarrow H + H$ ) is taken into account other than the charge exchange collision.

$$R \leq \nu_1(E_i)/\nu' \text{ (collision type 1)}$$

$$\nu_1(E_i)/\nu' < R \leq (\nu_1 + \nu_2)/\nu' \text{ (collision type 2)}$$

⋮

$$\sum_{j=1}^N \nu_j(E_i) / \nu' < R \text{ (null collision)}$$

$E_i$  : energy of the particle  $i$

$$\nu' = \max(n_T \sigma_T \nu)$$

$$\sigma_T = \sigma_1 + \cdots + \sigma_N$$

$\nu_j$  collision frequency for the collision type  $j$

$R$  : uniform random number

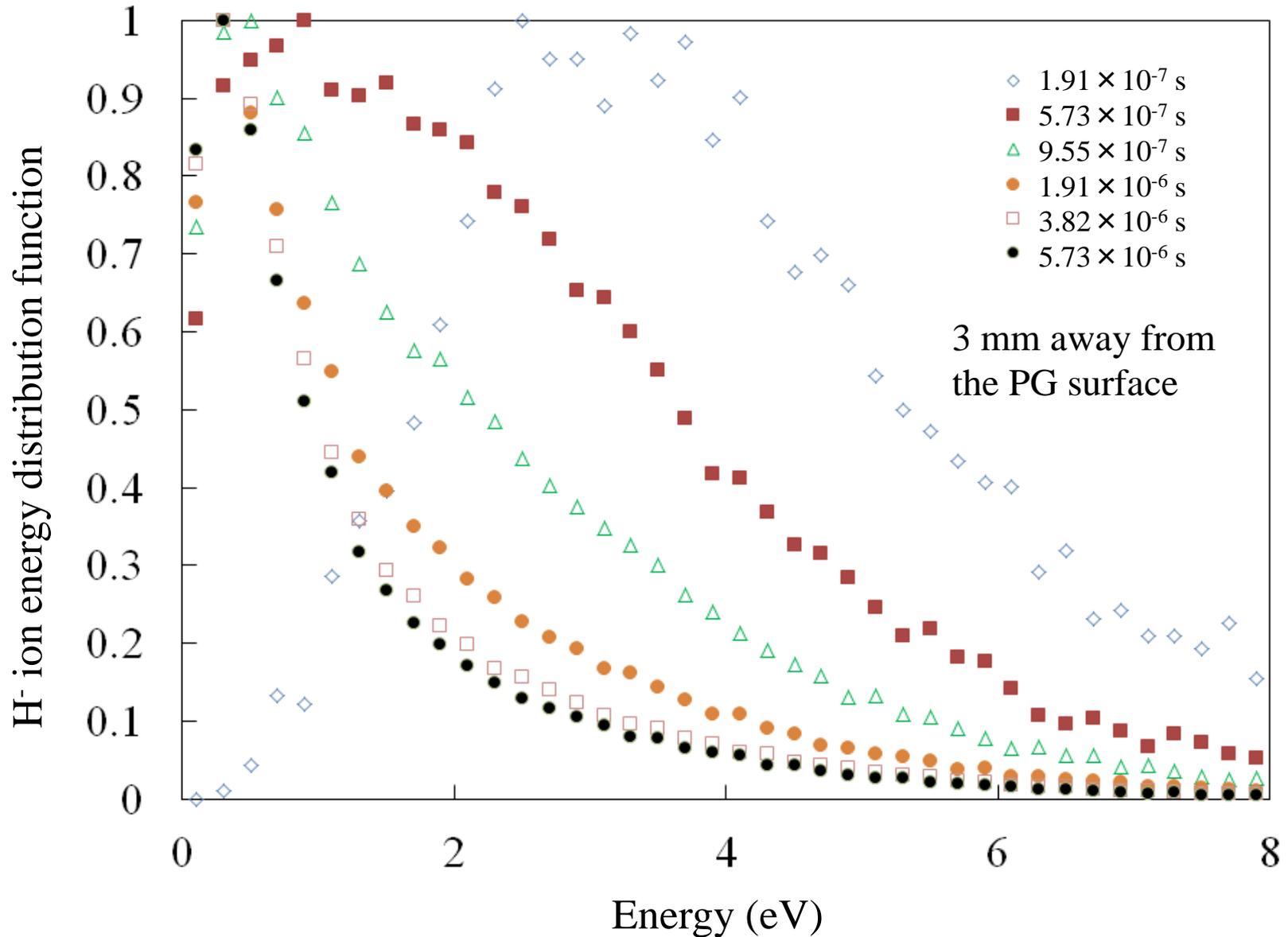
# Analysis of energy relaxation processes of H<sup>-</sup> ions

- Time evolutions of H<sup>-</sup> ion energy and velocity distributions will be shown.
- The energy relaxation process is analysed without H<sup>-</sup> ion extraction. Thus, the voltages of the PG, the EXG, the ESG, and the boundary of  $x = x_{max}$  are set to be zero.
- Moreover, the volume produced negative ions are not included in this analysis.

Initial number of super-particles

electron:  $N_e = 1.6 \times 10^7$ , H<sup>+</sup>:  $N_{H^+} = 1.6 \times 10^7$

# Time evolution of the H<sup>-</sup> ion energy distribution function with the Coulomb collision



# Estimation of the characteristic time of the energy relaxation due to the Coulomb collision

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The characteristic time of the energy relaxation due to the Coulomb collision is given by

$$\tau_{cc}^e = \frac{6\sqrt{3}\pi\epsilon_0^2 \sqrt{m_{H^-}} (kT_{H^-})^{1.5}}{q^4 n_{H^+} \ln \Lambda}.$$

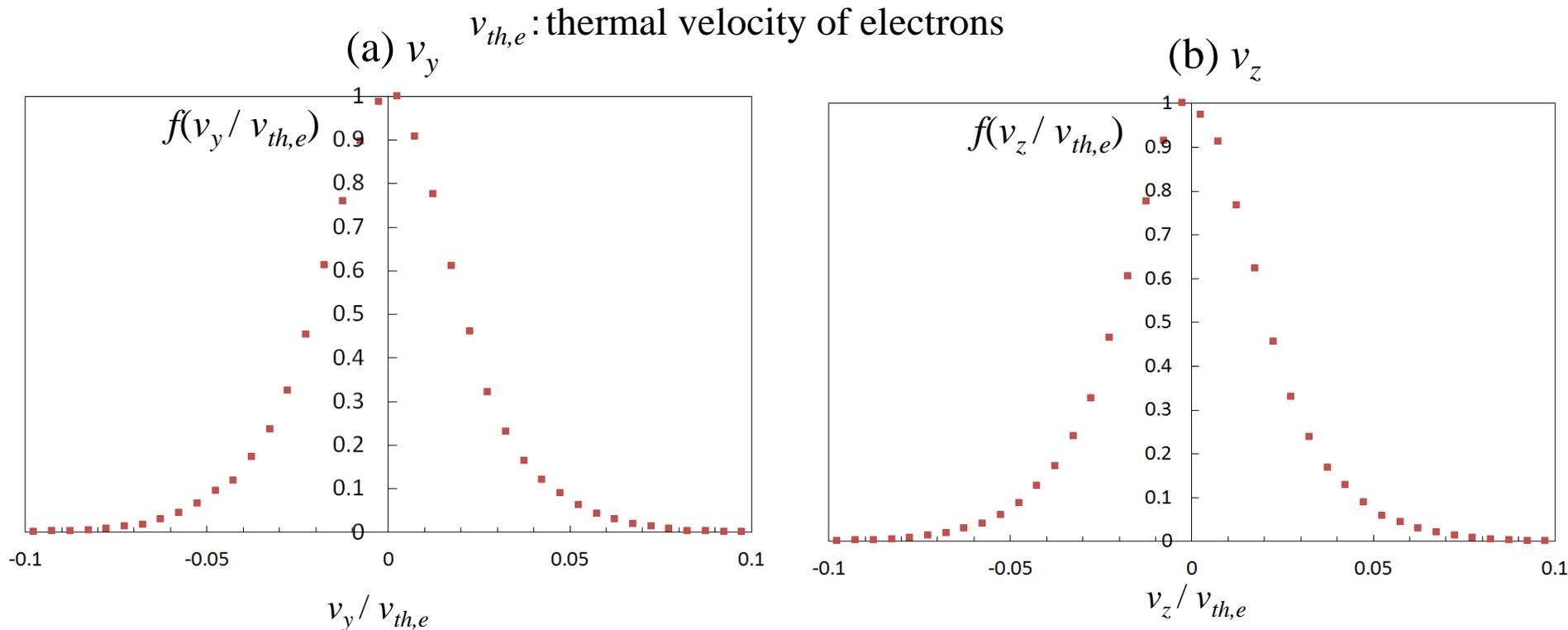
By substituting  $n_{H^+} = 1.0 \times 10^{18} \text{ m}^{-3}$ ,  $T_{H^-} = 1.5 \text{ eV}$  into the above equation,  $\tau_{cc}^e$  can be estimated to be  $1.87 \times 10^{-6} \text{ s}$ .

Thus, the simulation result agrees well with this estimated characteristic time of the order of the magnitude.

# The H<sup>-</sup> ion velocity distribution with the Coulomb collision

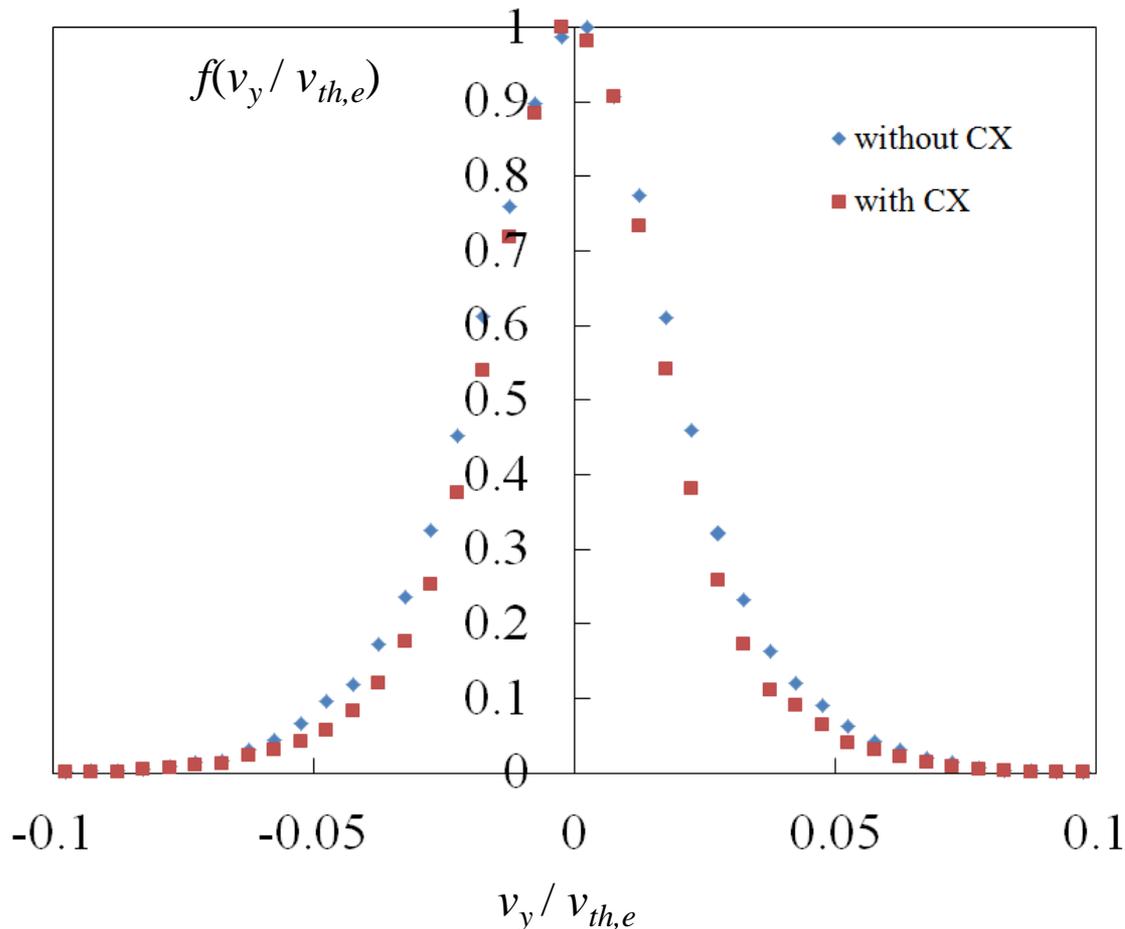
The H<sup>-</sup> ion temperature is reduced to 0.61 eV from 1.5 eV due to the Coulomb collision.

The H<sup>-</sup> ion velocity distribution functions perpendicular to the direction of H<sup>-</sup> extraction with the Coulomb collision



# Comparison of the H<sup>-</sup> ion velocity distribution with and without the charge exchange (CX)

It is indicated that the Coulomb collision is dominant for the energy relaxation under the present calculation condition ( $n_e = 1.0 \times 10^{18} \text{ m}^{-3}$ ,  $T_{H^+} = 0.25 \text{ eV}$ ,  $n_H/n_{H_2} = 0.5$ ,  $n_H = 9.4 \times 10^{18} \text{ m}^{-3}$ ,  $T_H = 0.1 \text{ eV}$ ).



$T_{H^-} \sim 0.61 \text{ eV}$  (without CX)

$T_{H^-} \sim 0.49 \text{ eV}$  (with CX)

At the energy of 1 eV, for example, each collision frequency is estimated to be

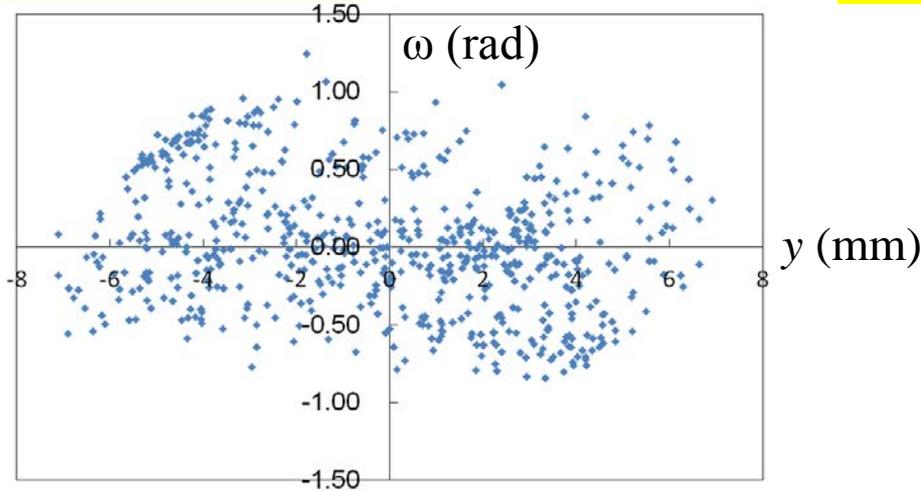
- Coulomb collision:  $9.82 \times 10^5 \text{ s}^{-1}$
- Charge exchange:  $1.84 \times 10^5 \text{ s}^{-1}$

# Analysis of the effect of the energy relaxation processes on the H<sup>-</sup> ion beam optics

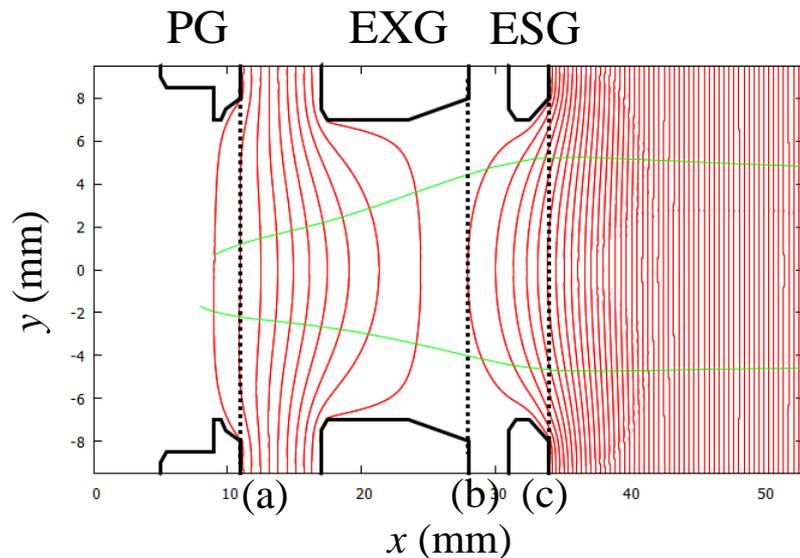
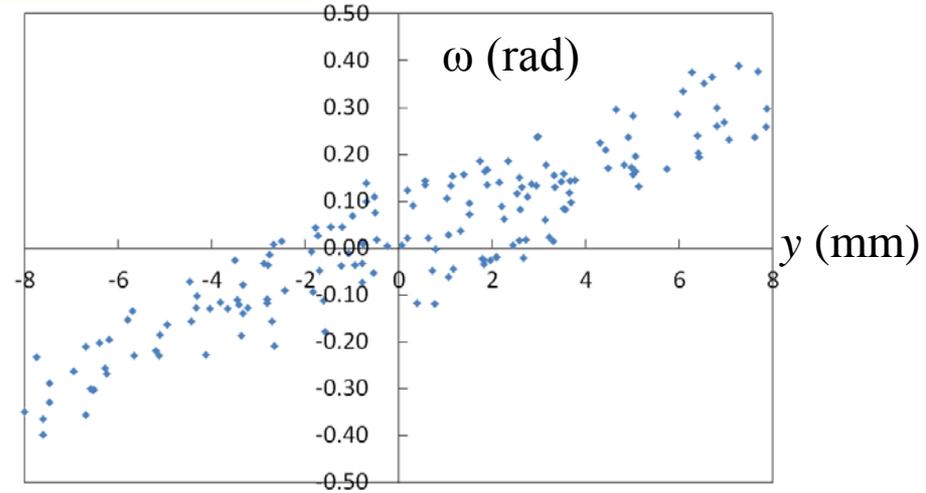
- Emittance diagrams without and with the energy relaxation processes will be compared.
- The voltages of the PG, the EXG, the ESG, and the boundary of  $x = x_{max}$  are applied. Each voltage corresponds to 0V (PG), 7.6 kV (EXG and ESG), and 52.4 kV (the boundary of  $x = x_{max}$ ).
- Initial number of super-particles  
electron:  $N_e = 2.96 \times 10^7$ , H<sup>+</sup>:  $N_{H^+} = 3.11 \times 10^7$ , volume produced H<sup>-</sup>:  
 $N_{H^-} = 1.56 \times 10^6$
- The H<sup>-</sup> ion beam current densities are estimated as follows:
  - (i) Only volume produced H<sup>-</sup> ions : 3 mA/cm<sup>2</sup>
  - (ii) volume + surface produced H<sup>-</sup> ions :  
without the energy relaxation processes : 16 mA/cm<sup>2</sup>  
with the energy relaxation processes : 21 mA/cm<sup>2</sup>

# Emittance diagrams of $H^-$ ions without energy relaxation

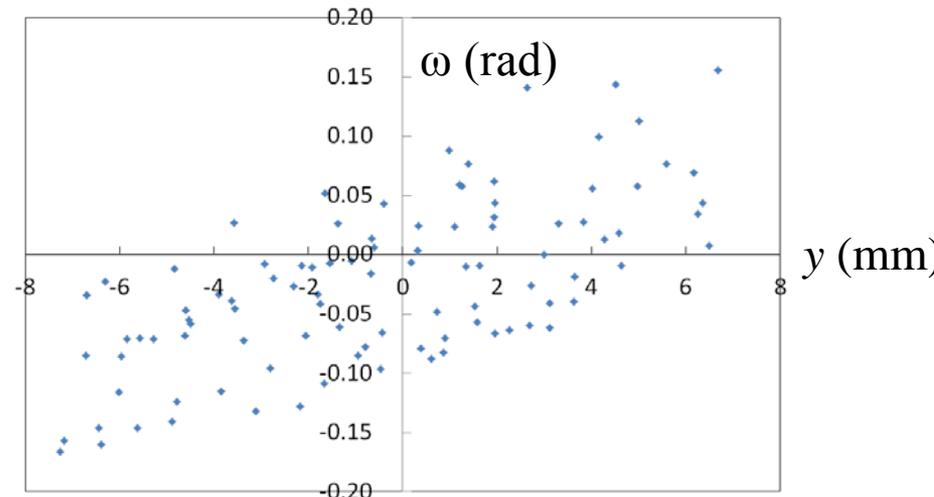
(a) Exit of the PG



(b) Exit of the EXG



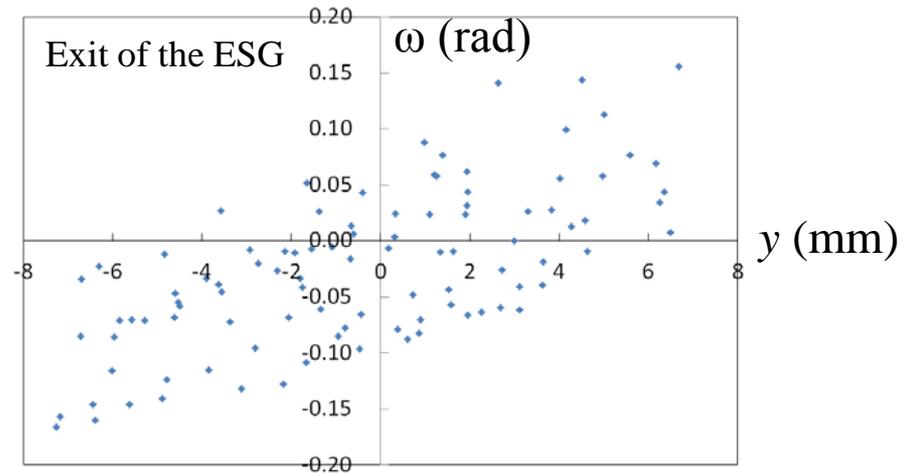
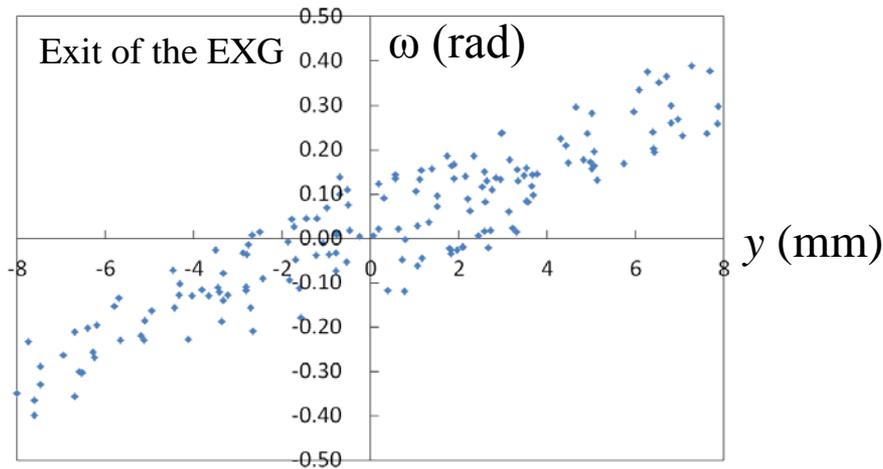
(c) Exit of the ESG



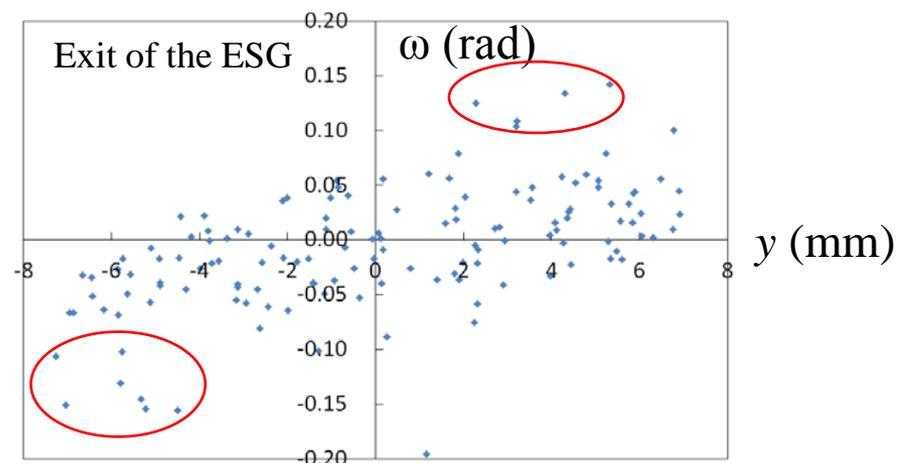
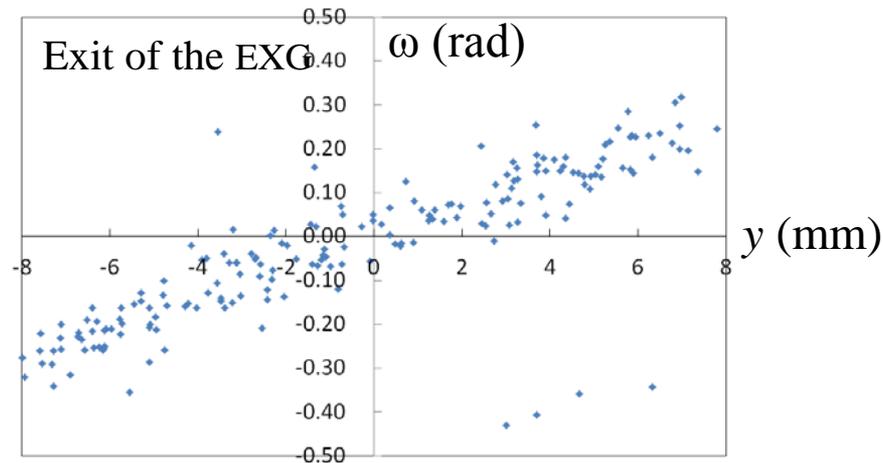
# Comparison of emittance diagram of H<sup>-</sup> (I)

It is shown that the emittances with the energy relaxation processes are smaller than those without the energy relaxation processes.

Without the energy relaxation processes

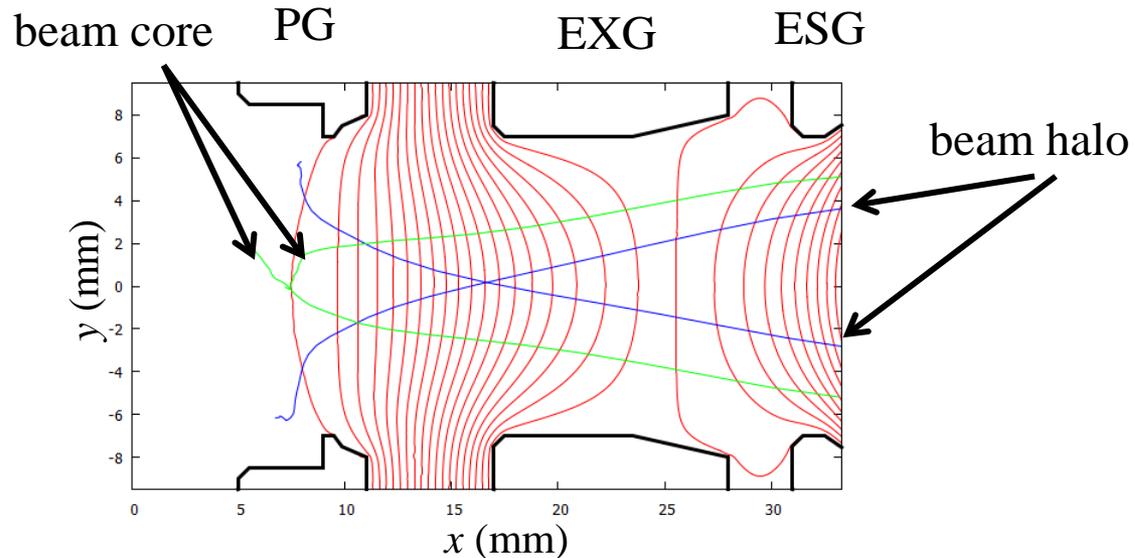
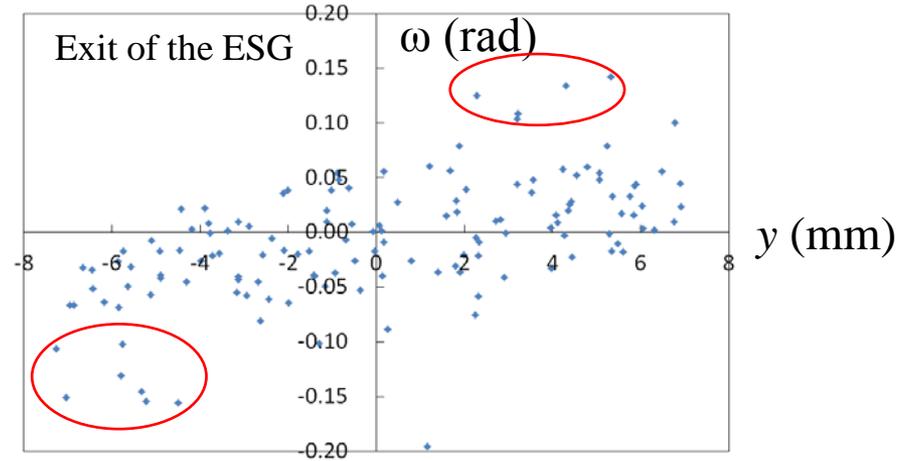


With the energy relaxation processes



# Comparison of emittance diagram of H<sup>-</sup> (II)

It is indicated that the separation of the beam core and the beam halo in the emittance diagram becomes clearer with the energy relaxation processes.



## Summary

We investigate the energy relaxation processes of  $H^-$  ions in a negative ion source, and the effect of these processes on the  $H^-$  ion beam optics by using the 3D3V PIC simulation.

- The energy relaxation of  $H^-$  ions due to the Coulomb collision and the charge exchange is verified ( $T_{H^-} = 1.5 \text{ eV} \rightarrow 0.49 \text{ eV}$ ).
- It is indicated that the Coulomb collision is dominant for the energy relaxation processes under the present calculation condition ( $n_e = 1.0 \times 10^{18} \text{ m}^{-3}$ ,  $T_{H^+} = 0.25 \text{ eV}$ ,  $n_H/n_{H_2} = 0.5$ ,  $n_H = 9.4 \times 10^{18} \text{ m}^{-3}$ ,  $T_H = 0.1 \text{ eV}$ ).
- It is shown from the emittance diagrams that the  $H^-$  ion beam optics is improved by the energy relaxation processes, and the separation of the beam core and the beam halo in the emittance diagram becomes clearer.

## Future Plane

The 3D3V PIC model will be extended to include the accelerator. The simulation results of the accelerated  $H^-$  ion beam emittance and the heat loads in the accelerator will be compared with the experimental results.